

Terascale turbulence computation using the FLASH3 application framework on the IBM Blue Gene/L system

*Understanding the nature of turbulent flows remains one of the outstanding questions in classical physics. Significant progress has been recently made using computer simulation as an aid to our understanding of the rich physics of turbulence. Here, we present both the computer science and the scientific features of a unique terascale simulation of a weakly compressible turbulent flow that includes tracer particles. (**Terascale** refers to performance and dataset storage use in excess of a teraflop and terabyte, respectively.) The simulation was performed on the Lawrence Livermore National Laboratory IBM Blue Gene/L™ system, using version 3 of the FLASH application framework. FLASH3 is a modular, publicly available code designed primarily for astrophysical simulations, which scales well to massively parallel environments. We discuss issues related to the analysis and visualization of such a massive simulation and present initial scientific results. We also discuss challenges related to making the database available for public release. We suggest that widespread adoption of an open dataset model of high-performance computing is likely to result in significant advantages for the scientific computing community, in much the same way that the widespread adoption of open-source software has produced similar gains over the last 10 years.*

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Introduction

Turbulent flows are ubiquitous in nature, arising at scales as small as tabletop experiments of fluids to scales as large as interstellar gas clouds, and they play a fundamental role in the mixing, transport, and combustion of fluids. However, despite its importance, turbulent behavior largely remains an unsolved problem, particularly when one is interested in computing detailed properties of a flow, such as the turbulent drag over an airplane wing, or the rate of combustion in a turbulent flame.

Over the last 20 years, scientific knowledge of turbulent flows has grown tremendously, partly because of the use of computers both in the laboratory and in simulation. Beginning in December 2005, the ASC (Advanced Simulation and Computing) Alliances Center for Astrophysical Thermonuclear Flashes at the University of Chicago was one of six groups in all fields of

computational science invited to use the Lawrence Livermore National Laboratory (LLNL) Blue Gene/L* (BG/L) supercomputer, shortly before it was permanently incorporated into its secure network. The BG/L system was the fastest computer in the world and largest in terms of processor number, at the time this paper was written. The simulation of the FLASH Center (ASC Alliances Center for Astrophysical Thermonuclear Flashes) is the largest weakly compressible, homogeneous, isotropic simulation in existence [1–3]. Approximately 1 week of CPU (central processing unit) time on 65,536 processors in coprocessor mode was used to complete the simulation, which was performed on a uniform mesh of 1,856³ grid cells, with fully periodic boundary conditions. (In coprocessor mode, one BG/L core is used for computation and a second is dedicated to communication.) The turbulence was also tracked with

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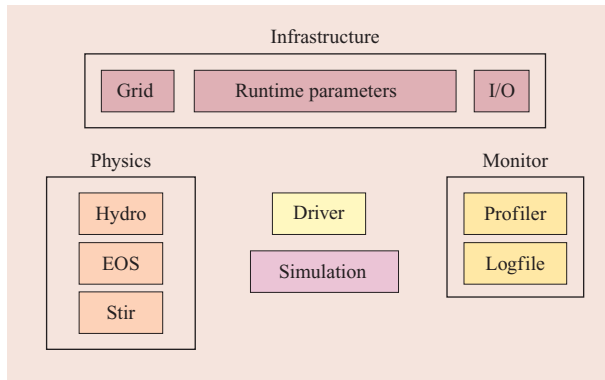


Figure 1

Examples of FLASH3 units.

256³ dimensionless Lagrangian particles. Our findings indicate that the wealth of data gathered is of very high quality and can be used to constrain fundamental theories of turbulence, as well as provide a “virtual turbulence laboratory” in which many other ideas (such as subgrid models of turbulence) can be tested. We plan to open the access to this dataset for the public by the end of 2007.

The FLASH code [4] used in this turbulence simulation is a modular, component-based application code used for simulating compressible, reactive flows found in astrophysical environments. The code supports multiple methods for managing the discretized simulation mesh, including our own uniform grid implementation, and makes use of PARAMESH (Parallel Adaptive Mesh Refinement) library [5], which implements a block-structured adaptive grid. The FLASH code scales very well (i.e., experiences a nearly linear speedup with increasing numbers of processors and with problem size) and was chosen in the spring of 2004 as one of the primary applications for the new BG/L platform. The BG/L machine demonstrates the utility of the massively parallel computing paradigm of large numbers of relatively slow and simple processors with limited memory. It provides teraflop-scale computation through duplication of hardware, rather than through hardware complexity. In its largest incarnation at LLNL, the parallelism is an order of magnitude greater than any other available platform. The configuration of BG/L represents a marked deviation from the prevailing practices in high-performance computing and presents opportunities and challenges to application developers and users. Because each BG/L processor offers lower performance and less memory than processors on other platforms, scientific applications attempting to effectively use this platform must be able to exploit fine-grained

parallelism while scaling to many tens of thousands of processors.

Architecture

The most recent major release of the FLASH code is version 3. The FLASH3 architecture is defined by two entities: the units and the setup tool. FLASH3 is neither a single application nor a single binary. Rather, it is a collection of units combined by the setup tool into an application tailored for specific simulations. The unit is the basic functional entity in FLASH3; it provides well-defined functionality and conforms to a structure that facilitates interactions with other units. All units must conform to a set of inheritance and encapsulation rules. For example, a unit may have subunits to collect self-contained subsets of its functionality into easily identifiable entities. A unit may also have interchangeable implementations of varying complexity, including child implementations that inherit from and override the functionality of the parent.

FLASH units can be broadly classified into five groups: infrastructure, physics, monitor, driver, and simulation (Figure 1). The *infrastructure units* are responsible for all the housekeeping tasks of the code such as managing the grid that describes the physical domain, making runtime parameters available as needed, and organizing all the I/O (input and output) from the code. The *physics units* implement algorithms to solve the mathematical equations describing specific physical phenomena. Physics units include *hydro* (for hydrodynamics) and *EOS* (the equation of state) [6]. The *stir* module is responsible for driving turbulent simulations to maintain a steady-state condition against viscous dissipation, which is described further below. The *monitoring units* *Logfile* and *Profiler* track the progress of an application, while the *driver unit* implements the time-advancement methods and controls the simulation by managing the interaction between the included units. The *simulation unit* is of particular significance because it specifies a given application by defining the initial conditions and simulation-specific runtime parameters.

Each unit has one or more text files called *config* files. These specify the (sub)unit requirements, such as physical variables, applicable runtime parameters, and the interaction with other code units. The setup script starts building an application by first examining the config file in the simulation unit, which specifies units essential to the simulation. The setup tool then parses the config files of required units to find their physical variables, runtime parameters, and necessary libraries in order to create a cohesive set of files defining an application. Finally, the user compiles the code pieces to produce an executable application for the problem. A user can replace any native FLASH routine by providing an alternative

implementation in the problem setup directory. For example, users can provide their own criteria for refining the mesh by including the appropriate code files with compatible function interfaces in the simulation directory.

Algorithms

The large-scale turbulence simulation described in this paper used a uniform Cartesian grid that divides the physical domain into uniformly spaced computational cells. Periodic boundary conditions are applied to all physical variables at the domain edges. Individual computational cells are grouped into equal-sized cubical subdomains, which are then mapped one-to-one to different processors. We refer to these subdomains as *blocks*. A perimeter of nonphysical guard cells surrounds each block of data, providing it with data either from the neighboring blocks (if the block is in the computational domain interior) or from boundary conditions (if the block lies on the edge of the computational domain).

The hydrodynamics solver used in the simulation is a directionally split piecewise parabolic method (PPM) [7] that solves the Euler equations with an explicit second-order accurate forward time difference [4]. Time-advanced fluxes at cell boundaries are computed using the numerical solution to the Riemann problem at each boundary. Initial conditions for each Riemann problem are determined by assuming the non-advanced solution to be piecewise-constant in each cell. Use of the Riemann solution has the effect of introducing explicit nonlinearity into the difference equations of flow and permits the calculation of sharp shock fronts and contact discontinuities without introducing significant nonphysical oscillations into the hydrodynamics. The flow variables are represented with piecewise parabolic functions, making this scheme a second-order accurate method.

Because theories of turbulence generally assume a steady state, and because turbulence is inherently a dissipative phenomenon, we have chosen to drive the simulation to sustain a steady state. This driving must be done carefully in order to avoid introducing artifacts into the turbulent flow. We use a relatively sophisticated stochastic driving method originally introduced by Eswaran and Pope [8]. The turbulent velocity fluctuations are described by Fourier-transforming from the spatial domain. For each “stirred” mode of the velocity field, an acceleration is applied at each timestep. The field consists of three complex phases, with each acceleration mode evolved by an Ornstein–Uhlenbeck (OU) random process, which is analogous to Brownian motion in a viscous medium. An OU process is a time-correlated, zero-mean, constant-root-mean-square process. Each subsequent step in the process adds a Gaussian random

variable with a given variance, weighted by a “driving” factor $\sqrt{(1-f^2)}$ for which $f = \exp(-\Delta t/\tau_{\text{decay}})$, and then causes decays in the previous value by an exponential factor f . Since the OU process represents a velocity, the variance is chosen to be the square root of the specific energy input rate divided by the decay time τ_{decay} . In the limit for which the timestep $\Delta t \rightarrow 0$, the algorithm represents a forcing term that is a linearly weighted summation of the old state with the new Gaussian random variable.

Evolving the phases of the stirring modes in Fourier space makes imposing a divergence-free condition relatively straightforward. At each timestep, the solenoidal components of the velocities are projected out, leaving only the noncompressional modes to add to the velocities. The velocities are then converted to physical space by a direct Fourier transform—adding the trigonometric terms explicitly. The transform is, therefore, trivially parallelized. Because the stirring is done in the low modes, the driving involves a fairly small number of modes, and so this decomposition is more efficient than a complete fast Fourier transform (FFT). The FFT would require large numbers of modes (six times the number of cells in the domain), the vast majority of which would have zero amplitude.

The simulation also evolved the movement of massless tracer particles, which are pointlike objects characterized by positions \mathbf{x}_i and velocities \mathbf{v}_i . The characteristic quantities of each particle are defined by the position of the particle and are determined by interpolation from the grid mesh. The particles move with the flow relative to the mesh and can travel from block to block, requiring communication patterns different from those used to transfer boundary information between processors for mesh-based data. The implementation in FLASH directionally splits the movement of particles out of a block. Consider a particle that moves from (x, y, z) to (x_1, y_1, z_1) . If the new coordinate x_1 is outside the current block of the particle, it is moved to the appropriate neighbor along the first dimension. The particle is now owned by the neighbor, and when examining movement along the second dimension, the neighboring block treats it identically to its own particles. This process is repeated for all the dimensions, until the particle terminates movement in the correct block. The direction-splitting halves the number of explicit data exchanges between processors per timestep from 26 (potentially one exchange with every neighbor including those along the corners) to 13. The computation required for a particle is performed by the same processor that evolves the block in which the particle resides. No effort is made to separately load balance the particle computations because experience has shown that the cost of load balancing the particles outweighs the gain of maintaining a good load balance

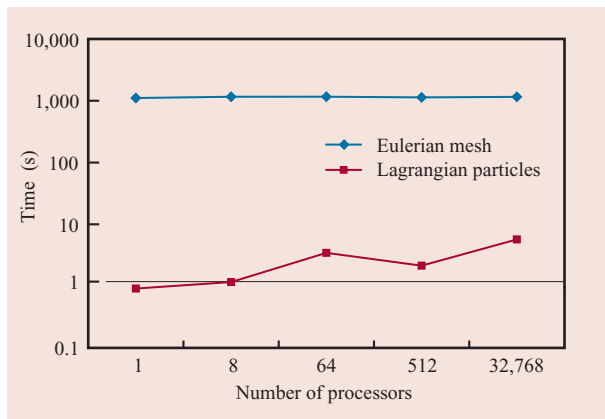


Figure 2

Weak scaling of the evolution of the Eulerian mesh and the Lagrangian particles with the FLASH3 code, for the driven turbulence problem.

for what is a small fraction of the overall execution time. The effect of this choice on scaling is discussed below. The time integration used for the Lagrangian particles in this simulation uses a predictor-corrector scheme that yields a second-order accurate solution for uniform timesteps.

Challenges of scale

As mentioned, the BG/L machine deviates from the current parallel computing norm of relatively few but very powerful processors with large memory. This standard model derives from cluster-based computing, which is driven by single-processing-element (PE) performance. The BG/L machine, on the other hand, uses slower processors with limited memory and relies upon finer-grain parallelism to achieve performance. This shift in the computing paradigm presents major challenges for codes that are memory intensive and have components with global communication patterns.

Implementation of multiphysics codes such as FLASH3 usually face trade-offs between modularity, efficiency of memory, and CPU usage. For example, in order to keep various physics solvers in the code independent of one another, and their data management well modularized, multiple copies of some datasets may exist in the code. This problem could be alleviated with dynamic memory management, but this solution causes loss of compiler optimizations and, therefore, loss of computational efficiency. Also, while a single timestep evaluation typically involves only nearest-neighbor communications, some operations are necessarily global, such as updating the timestep selected by the Courant condition. Additionally, scientific calculations generate

massive amounts of data, and the I/O management and post-processing can easily become a significant challenge.

Because turbulent flow simulations benefit from high resolution at all locations, the simulation described here did not require use of the adaptive mesh capabilities of the FLASH code [9]. Use of a uniform grid reduced the global communication complexity of the Eulerian part of the solution, allowing it to scale almost perfectly, as shown in the weak scaling plot of **Figure 2**. A *weak scaling study* is one in which researchers vary the problem size and the number of processors simultaneously, such that the problem size per processor remains constant. Figure 2 is a plot of the time required to advance the solution by 50 timesteps; both axes are in log scale. The two lines show the overall evolution time for the turbulent flow simulation and the time taken by the tracer particles to evolve forward in time by advancing their position and velocity vectors. The number of processors along the x-axis grows from 1 to 32,768, and the amount of work grows in proportion to the number of processors. The Lagrangian tracer particles, however, do not show the same perfect scaling as that observed for the grid evolution, even though their communications pattern is nearest-neighbor, like that of the Eulerian grid. As mentioned above, no separate effort is made to load balance the particles. The complex nature of the turbulent flow changes the particle distribution during the evolution, which unbalances the particle load distribution and degrades the scaling. However, because the particles account for only a small fraction (<0.3%) of the overall execution time, the effect on the overall scaling is negligible.

Despite the excellent overall scaling, the sheer scale of the simulation and the tremendous amount of generated output data still presented a huge challenge. Before the run, we were careful to test the scaling of the FLASH3 I/O, given the lack of evidence for successful parallel I/O on the BG/L machine or on other such large-scale computations. As anticipated, we found that none of the parallel I/O libraries available with FLASH3, i.e., HDF5 (hierarchical data format), PnetCDF (parallel-net common data format), or basic MPI-IO (messaging-passing interface I/O), scaled to more than 1,024 processors. This limitation required us to implement a direct I/O approach whereby each process wrote its portion of the global data to its own file in the Fortran sequential format. The simulation corresponded to approximately 2,300 separate data dumps in time, and each dump created 32,768 files, for a total of roughly 74 million files, occupying 154 TB (terabytes) of disk capacity. Here, the challenge involved not only the volume of data, but also the almost unmanageable number of files. The transfer of data to the local site for analysis took several weeks, using four nodes of the

LLNL machine ALC, each running the Globus Toolkit** protocol *gridftp*. As background, ALC is a large Linux** cluster that uses IBM xSeries* servers, and the Globus Toolkit is an open-source software toolkit used for building grids. The total sustained transfer rate averaged about 20 MB/s. We are now using computing clusters to visualize and analyze the data, which has become a large-scale computing project of its own.

Science

Introduction

The single most significant contribution to turbulence theory was Kolmogorov's 1941 idea that at very high Reynolds numbers, turbulent flows develop an energy cascade from large scales down to small, which is governed by self similarity [10]. The range of scales between the large modes where the fluid is driven and the small scales on which its energy is dissipated is known as the *inertial regime*. According to Kolmogorov, the high-Reynolds-number turbulent flow is said to be "universal"; that is, the resulting state of any two such fluids is governed by the same set of scaling laws in the inertial regime.

Over the past 20 years, extensive research has been performed on turbulent flows. One of the key insights attained in experiment and in numerical simulation is that Kolmogorov's original theory is incomplete: The hypothesized self similarity is not observed because the dissipation within the fluid does not occur homogeneously, but instead it is intermittent in both space and time. The resulting scaling laws, which differ from Kolmogorov's theory, are said to describe *anomalous scaling*.

Kolmogorov's theory relates to turbulence in the same manner as Newton's laws relate to mechanics. They both provide highly successful, though incomplete frameworks whose enormous influence is widely felt. A number of phenomenological theories have been advanced as possible heirs to Kolmogorov's legacy, although it remains unclear which of these (if any) is correct [11, 12]. Working directly from the Navier–Stokes equations presents challenging barriers to standard mathematical analysis techniques; thus, theorists must instead work from plausible assumptions.

Because our techniques of treating hydrodynamic flows away from the strictly incompressible limit is different from the majority of work done in the turbulence community, we also must compare our results with experiment, theory, and previous simulations in order to convince ourselves that weak compressibility does not have a strong influence upon the scientific conclusions we draw from our dataset. In the following section, we use

the idea of anomalous scaling to probe our BG/L turbulence run dataset to gather clues to these issues.

Results

A fundamental mathematical tool commonly used by turbulence researchers to examine the scaling properties of turbulent flow is the p th-order structure function $S_p(r)$, which is closely related to the autocorrelation function of the velocity field:

$$S_p(r) = \langle |\vec{v}(\vec{x} + \vec{r}) - \vec{v}(\vec{x})|^p \rangle \propto r^{\zeta_p}.$$

Here $\langle \rangle$ denotes an average of spatial locations \vec{x} over all space and ζ_p are the scaling exponents. The proportionality on the far right-hand side applies over a range of separations r in the inertial regime and is a direct consequence of self similarity.

A naive computation of $S_p(r)$ involves an average over all spatial points. However, instead of calculating $S_p(r)$ directly, we generate probability distribution functions (PDFs) of each component of the velocity increment $\Delta v_r = \vec{v}(\vec{x} + \vec{r}) - \vec{v}(\vec{x})$ of each interval r for each dimension for each dimensional velocity component. Because this approach involves only the calculation of the separations along a given dimension, it allows for a natural slab decomposition of the domain of a given timestep, as well as very straightforward parallelization, enabling us to perform this analysis on a small cluster. Once the PDFs of velocity increments are generated, the structure functions can be computed directly from

$$S_p(r) = \int d\Delta v_r P(\Delta v_r) \Delta v_r^p.$$

Here, we denote the probability distribution function of the velocity increment Δv_r on the increment r by $P(\Delta v_r)$. The Lagrangian tracer particle data can be analyzed in a similar fashion, making use of the p th-order structure function with respect to time:

$$S_p(\tau) = \langle |\vec{v}(t + \tau) - \vec{v}(t)|^p \rangle \propto \tau^{\zeta_p}.$$

While the Lagrangian dataset is significantly smaller, problems in the calculation do arise because each timestep is contained in a different file, making I/O much more costly due to the frequency of accesses than observed for the Eulerian dataset. A similar method of probability distribution function generation is utilized as was described above. The structure-function data generated from this set was then used to verify the Lagrangian tracer particle data.

A useful technique for determining the scaling exponents ζ_p was first discovered by Benzi et al. [13], who noted that an extended self-similar region appears when, instead of plotting $S_p(r)$ for different values of r , a plot is used in which the vertical and horizontal axes are

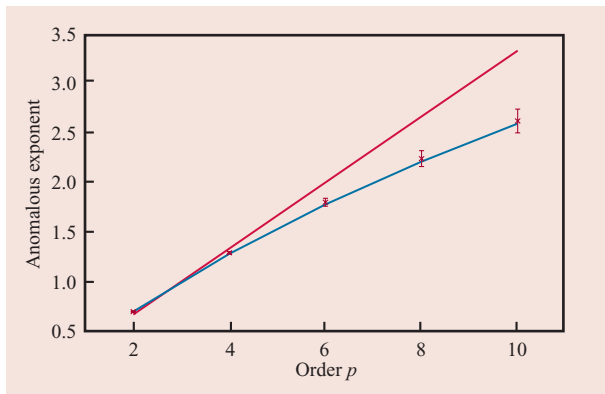


Figure 3

Comparison of anomalous exponents for theory and experiment. Anomalous scaling exponents (for $p \leq 10$) are shown for the BG/L run (points with error bars) and are compared against predictions of Kolmogorov's original 1941 theory (red straight line), as well as the predictions of She–Leveque (blue curved line). When plotted at the resolution of this graph, the experimental results of Benzi are indistinguishable from the points plotted for the BG/L run.

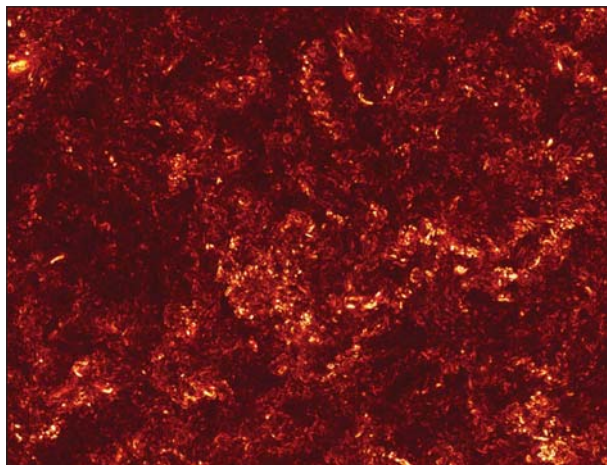


Figure 4

A 2D slice through the computational domain, depicting the wealth of turbulent structures realized in the simulation. The color shading is a nonlinear mapping of the density gradient within the plane and is constructed to emphasize density structures, which are unique signatures of weakly compressible turbulence.

structure functions. This technique is referred to as *extended self similarity* (ESS). The scaling exponents derived from ESS are identical to the ζ_p above, because the third-order structure function $S_3(r)$ is exactly proportional to r , as was first rigorously demonstrated by Kolmogorov in his famed 4/5th law. ESS has an advantage because the self-similar scaling regime is

broadly extended over one to two more decades in length scale, which permits much more precise determinations of the scaling law exponents.

One can easily demonstrate that if Kolmogorov's original theory were strictly correct, and if dissipation occurred homogeneously, the exponents ζ_p would simply equal $p/3$. In the inertial regime, the flow is self similar and no other characteristic length scales are introduced. Therefore, the scaling exponents ζ_p follow directly from simple dimensional analysis: Assuming a characteristic velocity v over a spherical region of size r , the dissipation per unit mass ϵ within r must scale as $\epsilon \propto v^3/r$. If ϵ is homogeneous and the flow is steady, one infers that $v \propto r^{1/3}$. Dimensional analysis then reveals that the exponents ζ_p are simply equal to $p/3$.

We can directly test Kolmogorov's original theory, as well as more recent theories, by applying ESS to the data from the BG/L run. The results are shown in **Figure 3**. Here, we observe the scaling exponents ζ_p versus p (derived from fits of the structure function) as a function of separation r along x —one of the three principal components of the longitudinal structure function. As is easily seen, Kolmogorov's 1941 theoretical prediction [10] deviates systematically from both Benzi's experimental analysis [13] and our simulation. In contrast, the more recent theory of She and Leveque [12] is in close agreement with both experiment and simulation. We conclude that despite being weakly compressible, the results of our simulation agree very well with previous incompressible results and suggest that our dataset can be used to explore a wide variety of issues in turbulent flows.

Visualization

Current visualization efforts have focused on exploration of the dataset. In order to meet analysis needs, this effort has utilized a combination of open-source solutions (e.g., the parallel visualization tools Para View and VisIt) and more specific solutions. Processing has been performed to augment the dataset with post-simulation content such as scalar magnitudes of the local vorticity and divergence vectors. This data is now being stored as part of the dataset that will be made publicly available. Visualization challenges have demonstrated the need for large computational resources beyond the initial simulation, for data-filtering and data-selection tools to reduce the data to appropriate amounts for viewing, and for investment in remote visualization solutions. The generation of the derived data fields for vorticity and divergence required 1.5 days on a 64-node cluster. Visualizing all 16 million Lagrangian particle traces yields no useful insight. Instead, filtering and cutting (i.e., slicing) the data and using nonlinear shading functions to highlight features of interest are crucial (**Figure 4** and **Figure 5**). Future efforts will involve the integration of

workflow tools for the construction of analysis pipelines and the availability of specific tools to enable users to visualize the data.

Open dataset model

The public release of the dataset will perhaps be one of the most far-reaching consequences of this effort. Performing simulations on machines with teraflop or petaflop performance is by necessity a major challenge that few research efforts have both the technical capacity and the computational resources to address. Even when successful, the appropriate datasets are not typically released publicly, which limits their impact on the few researchers who have access to the data. Here, we draw inspiration from the open-source movement and advocate an open model for high-performance computing datasets—i.e., that large-scale high-performance computing datasets should be made openly accessible. While dissemination and analysis of high-performance computing datasets pose numerous technical challenges, we argue that these technical challenges can be addressed and overcome and are outweighed by the potential scientific gains to be achieved by sharing the datasets.

Historically, the movement known today as *open source* originated with the IBM user group SHARE in the 1950s and was later championed by Richard Stallman and the Free Software Foundation beginning in the early 1980s. However, it first received widespread attention following Eric Raymond's highly influential book *The Cathedral and the Bazaar* [14], which inspired the Netscape company to release a version of its browser software in 1997.

The open-source model of distributing source code has had an enormous impact on computing in both the scientific and the business world. At the heart of the open-source paradigm is the elimination of barriers to the exchange of source code, thereby creating a free marketplace of ideas wherein communication and resource sharing are encouraged. In the years following Raymond's essay, the number of open-source code development projects quickly increased, and companies such as IBM, Hewlett-Packard, Oracle, and CollabNet have incorporated the open-source paradigm into their business models. Perhaps even more far reaching is the wide array of other endeavors inspired by the open-source paradigm—including examples ranging from open publication projects such as Wikipedia**, the Creative Commons, and the Science Commons to open educational curricula, such as that facilitated by the OpenCourseWare project at MIT, as well as numerous other projects.

We reiterate our belief that the same open-minded thinking that gave rise to the open-source model of distributing source code can also be profitably applied to

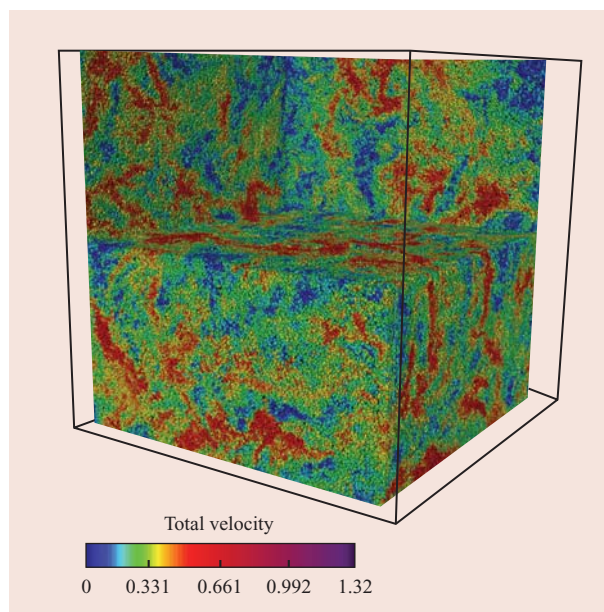


Figure 5

Particles contained within cut planes of the problem domain in fully developed turbulence, shaded by velocity. (Velocity values are relative to the speed of sound, which is set to 1.)

large-scale high-performance computing datasets. In other areas of science in which experimental and observational datasets have been made open (i.e., available) to researchers, enormous strides have been made. Particularly successful examples include the Human Genome Database, the Sloan Digital Sky Survey, and the Particle Physics Data Grid. The impact of these projects has been enormous in their respective fields. More than 3,000 astrophysics articles refer to the Sloan Digital Sky Survey alone. However, despite the significant advantages to be gained by sharing their data, the high-performance computing community has lagged behind their colleagues in opening access to their datasets. We believe this is in part due to some lingering fundamental misconceptions about the nature of simulation and analysis. Once these issues are recognized, it becomes clear that opening access to high-performance computing datasets presents a major opportunity for the growth of computational sciences in the near future.

The first common misconception is that large-scale computational datasets, which required the largest supercomputers in the world to compute, would also necessarily require the largest supercomputers to store and to analyze. However, this is not necessarily the case. For a wide class of problems that are CPU bound (and not memory bound), the results of large-scale simulations performed on the largest machines can be analyzed on

smaller machines, such as the widely available small-scale Linux clusters. As a concrete example, consider a traditional high-performance computing, time-dependent simulation of a set of partial differential equations discretized explicitly onto a uniform mesh of N^D cells in D dimensions. In this case, because of the Courant limitation on the timestep, the number of CPU operations to complete the simulation will scale as N^{D+1} , even though the number of operations to be performed for a local analysis scales only as N^D . On the basis of this analysis, it is easy to see that local post-processing of a dataset will be decreased roughly by a factor of N over the full simulation. In state-of-the-art three-dimensional (3D) simulations, N approaches 2,000 to 4,000, and the number of CPUs utilized during the full simulation may be as large as 10^5 . However, by simply scaling these numbers, it is clear that the post-processing analysis of this same dataset can be completed in a roughly equal amount of wall-clock time on just a few hundred processors. Significantly, as we suggested, analyses of large-scale datasets can be completed on small-scale clusters. In fact, the analysis shown in this paper was completed on several small-scale Linux clusters at the University of Chicago, all with fewer than 256 processors.

Another common misconception is that distribution of large-scale datasets could possibly use a significant amount of bandwidth and take very long times to transfer. However, this is also not a fundamental deterrent. For instance, one solution is simply to sidestep the transfer of the datasets and colocate storage and computation, allowing open access to the system to all interested parties. We believe that this is the natural solution for terabyte and larger datasets, and we have adopted the colocated model in establishing a new datastore system at the University of Chicago. Our turbulence dataset will be served to the community from the Computation Institute (CI) large datastore at the University of Chicago. The system is a scalable high-performance storage resource that has 75 TB of storage configured in an 8+2 RAID array, allowing up to 48 drives to fail with no impact on performance, stability, or reliability. The system can deliver a sustained throughput of 3 GB/s. It can also be scaled to 480 TB of storage. Five I/O servers are connected to the storage system by five fiber channels and then connected to outside the datastore via 1-Gb/s Ethernet connections to the 10-Gb/s I-WIRE link of the CI. As background, note that I-WIRE is a dark fiber communications infrastructure interconnecting organizations that include Argonne National Laboratory, the University of Illinois, the University of Chicago, the Illinois Institute of Technology, Northwestern University, and the Illinois Century Network Chicago hub. Collocated with the storage resource is the CI TeraPort compute resource,

which is a 244-processor AMD Opteron** computing cluster used for local processing of the data. High-performance computing consists of a hierarchy of computation, ranging from the fastest machines in the world used by a handful of researchers to smaller machines accessible to a much wider community. The public release of the FLASH Center dataset will amplify the impact of our turbulence effort significantly by allowing us to share our results with many levels on the computational hierarchy. Moreover, if our data dissemination effort is successful, it will provide both a fruitful model and concrete software tools that will encourage computational scientists to release their datasets in a similar fashion.

Conclusion

The ASC FLASH Center at the University of Chicago has produced the largest weakly compressible, homogeneous isotropic turbulence simulation to date. The simulation was performed on the BG/L, the fastest supercomputer, located at the LLNL. The results were produced using the newly released version 3 of the FLASH code, which is a modular, application-specific tool for astrophysical simulations that scales well to massively parallel environments. The BG/L configuration of more than 64,000 processors with limited memory and computing power posed special challenges. Specialized I/O routines were developed, and efficient particle-tracking schemes were implemented. Despite the demanding conditions, preliminary analysis of the results indicates a dataset of very high quality. Results of extended self-similarity analysis on the data show support for new theories of turbulent structure and match well with experimental evidence. The massive dataset will be released to the public, thereby further expanding the impact of this simulation.

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